

## PROBLEMS OF STANDARDISING ILLUMINATION FOR PLANTS IN GREENHOUSES AND GREEN STRUCTURES

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**Abstract.** Today greenhouses are transformed. In the middle of the past century, they were almost glazing buildings above the ground. Due to the development of planting technologies, including mats or trays with substratum, aero – and hydroponics, etc., greenhouses now can be anywhere, including underground. This gives impetus for urban agriculture with optimal logistics (growing near consuming). Indoor green structures become more and more popular. The illumination of them is very important because plants lose decorative properties in unfavourable conditions. At the beginning of this century, there was an analysis of a lot of failed attempts to create winter gardens on underground floors. The illumination was calculated successfully by today's norms, but the plants withered. This is because the norms were developed for natural-illumination greenhouses. Usually, the illumination is measured in lux or  $\mu\text{mol}/\text{day}$ . The first unit is weighted by wavelength according to the people's eyes sensitivity. The second one accumulates all photons. But the plants have another photosynthetic activity curve. They use two photosynthetic substances – chlorophyll and beta-carotenoid (active on the green light). The chlorophyll changes its absorption curves dependent on solvent presence (a and b). This allows some variability for adapting to the light spectrum, which is used by water plants. Thus, both units do not apply to artificial illumination. In this work, we analyse the curves of solar and phytolamp spectrums, averaged sensibility and spectral luminous efficiency for photopic vision. Integration of the curves allows recalculation of the lux-meter reading to the equivalent solar illumination or the last one to the phytolamp power. We propose a new unit system – phytocandela-phytolumen-phytolux – according to the photosynthesis efficiency curve that is numerically equal to candela-lumen-lux under sunlight. This shows that lux may not be a base unit because it is related to a single biological species but not a physical property.

**Keywords:** greenhouse; illumination; phytolamp; lux; photosynthesis.

### Introduction

Today greenhouses are transformed. In the middle of the past century, they were almost glazing buildings above the ground. Due to the development of planting technologies, including grows on artificial substratum [1] in mats or trays [2], aero – [3] and hydroponics [4], etc., greenhouses now can be anywhere, including underground. This gives impetus for urban agriculture [5] with optimal logistics (growing near consuming). Indoor green structures and indoor greening become more popular [6,7]. The illumination is very important as plants lose decorative properties in unfavourable conditions. Outdoor green structures are promising places for urban agriculture with different benefits for buildings [8-12]. Nevertheless, they are dependent on seasons, but indoor agriculture gives harvest year-round. The authors perform systematic laboratory tests and theoretical investigations [12] with outdoor and indoor green structures using wind tunnels and special mathematical approaches [13]. The research gives a possibility to calculate the energy and indoor air quality benefits for a building by using outdoor green structures and other-purpose premises for agriculture.

At the beginning of this century, the authors' analyses of a lot of failed attempts to create winter gardens on underground floors were performed. The illumination was calculated successfully by today's norms, but the plants withered. This is because the norms were developed for natural-illumination greenhouses, but fluorescent lamps with different spectra were used. Now, LED phytolamps are more effective due to the optimised spectrum. They are different – red and blue or full-spectrum. Usually, the illumination is measured in lux [14] or  $\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$  [15]. The first unit is weighted by wavelength according to the people's eyes sensitivity. The second one accumulates all photons. But the plants have another photosynthetic activity curve. They use at least two photosynthetic substances – chlorophyll (a or b dependent on solvents) and beta-carotenoid (active on the green light) [16]. This allows some variability for adapting to the light spectrum, which is used by alga. Thus, both units are not applicable to artificial illumination. We should propose a new photometric unit for plants. As there are no special measuring devices, we should measure this value by a commonly used and cheap lux-meter or pyranometer with additional recalculations.

## Materials and methods

We should analyse the curves of solar and phytolamp spectrums, photosynthetic action spectrum and spectral luminous efficiency for photopic vision (Fig. 1).

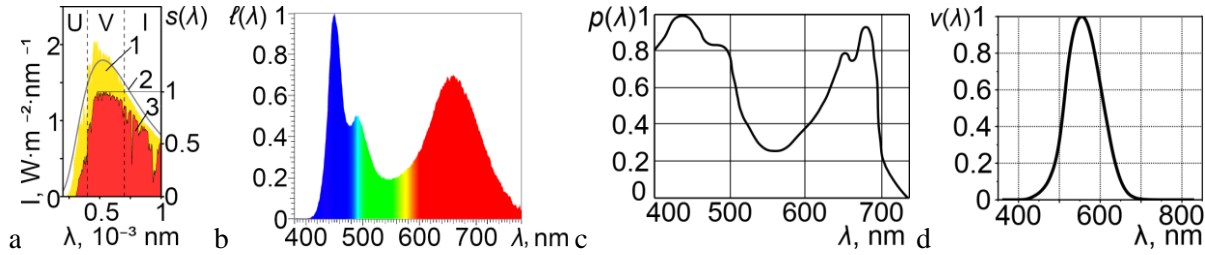


Fig. 1. **Spectrums:** a – fragment of solar radiation spectrum  $s(\lambda)$  [17]; b – phytolamps spectrum  $\ell(\lambda)$  based on LED 2835 growing [18]; c – photosynthetic action spectrum  $p(\lambda)$  [19]; d – spectral luminous efficiency for photopic vision  $V(\lambda)$  by the tabular data in [20]: 1 – above the atmosphere; 2 – 5778 K blackbody; 3 – at the sea level; U – ultraviolet; V – visible; I – infrared

LEDs (or other light sources) have a specific spectral radiation density of  $0 \leq \ell(\lambda) \leq 1$ . Spectral density of irradiance of a surface,  $W \cdot m^{-2}$ , if the maximum of it is  $E_{e,\lambda}(\lambda_{m,\ell})$ ,  $W \cdot m^{-2}$ ,

$$E_{e,\lambda}(\lambda) = E_{e,\lambda}(\lambda_{m,\ell}) \cdot \ell(\lambda). \quad (1)$$

Using spectral luminous efficiency for photopic vision  $0 \leq V(\lambda) \leq 1$  and a conversion factor  $K_m$ ,  $lm \cdot W^{-1}$ , the illuminance, lux, can be found by integration from minimum  $\lambda_{min}$ , nm, to maximum  $\lambda_{max}$ , nm, wavelength of the photosynthetic action spectrum, as (Fig. 1 c,d) outside the range  $V(\lambda) \approx 0$  taking into account equation (**Error! Reference source not found.**):

$$X = K_m \cdot \int E_{e,\lambda}(\lambda) \cdot V(\lambda) \cdot d\lambda = K_m \cdot E_{e,\lambda}(\lambda_{m,l}) \cdot \int \ell(\lambda) \cdot V(\lambda) \cdot d\lambda. \quad (2)$$

The illuminance, lux, for solar radiation with specific spectral radiation density  $0 \leq s(\lambda) \leq 1$ , the irradiance of the surface  $E_{e,\lambda,s}(\lambda)$ ,  $W \cdot m^{-2}$  and the maximum of it  $E_{e,\lambda,s}(\lambda_{m,s}) W \cdot m^{-2}$

$$X_s = K_m \cdot E_{e,\lambda,s}(\lambda_{m,s}) \int s(\lambda) \cdot V(\lambda) \cdot d\lambda. \quad (3)$$

Let us introduce a new reduced photometric value system – phytocandela-phytolumen-phytolux – according to the photosynthesis efficiency curve, which is numerically equal to candela-lumen-lux under sunlight. This will leave the old recommendations intact. Using the conversion factor  $K_{ph}$ ,  $phlm \cdot W^{-1}$ , we have illuminance, phlux

$$X_{ph} = K_{ph} \cdot E_{e,\lambda,s}(\lambda_{m,s}) \int s(\lambda) \cdot p(\lambda) \cdot d\lambda. \quad (4)$$

By the definition,  $X_s = X_{ph}$  at the same  $E_{e,\lambda,s}(\lambda_{m,s})$ , so by equations (5) and (6),  $phlm \cdot W^{-1}$ ,

$$K_{ph} = K_m \cdot \int s(\lambda) \cdot V(\lambda) \cdot d\lambda / \int s(\lambda) \cdot p(\lambda) \cdot d\lambda. \quad (5)$$

If we create a phytolux-meter with the sensitivity curve as  $p(\lambda)$  and the conversion factor  $K_{ph}$  we will obtain analogically to expression (4),  $W \cdot sr^{-1} \cdot m^{-2}$

$$X_{ph} = K_{ph} \cdot E_{e,\lambda}(\lambda_{m,l}) \cdot \int \ell(\lambda) \cdot p(\lambda) \cdot d\lambda. \quad (6)$$

And finally, we can use the equation system (4) and (9) to convert lux to phytolux

$$X_{ph} = \kappa \cdot X, \quad (7)$$

where  $\kappa$  – converting factor specific for a light source,  $phlux \cdot lux^{-1}$ :

$$\begin{aligned} \kappa &= X_{ph}/X = K_{ph} \cdot \int \ell(\lambda) \cdot p(\lambda) \cdot d\lambda / (K_m \cdot \int \ell(\lambda) \cdot V(\lambda) \cdot d\lambda) = \\ &= (\int s(\lambda) \cdot V(\lambda) \cdot d\lambda \cdot \int \ell(\lambda) \cdot p(\lambda) \cdot d\lambda) / (\int \ell(\lambda) \cdot V(\lambda) \cdot d\lambda \cdot \int s(\lambda) \cdot p(\lambda) \cdot d\lambda). \end{aligned} \quad (8)$$

Integration of the curves in equations (2-8) can be done numerically in two ways. The first is tabulating of the graphical data in Fig. 1 with a very fine step and numerical integration of the tabular data. This way is very time-consuming. A more effective approach is vectorising Fig. 1 a-c. SVG graphics are used, which contain a plain text description of each line. It can be done by open-source software (in this work – Inkscape). The file has a “path” command for Bezier [21] splines using linear  $B(t) = (1-t) \cdot P_0 + t \cdot P_3$ , square  $B(t) = (1-t)^2 \cdot P_0 + 2 \cdot (1-t) \cdot t \cdot P_1 + t^2 \cdot P_3$ , and cubic segments

$$B(t) = (1-t)^3 \cdot P_0 + 3 \cdot (1-t)^2 \cdot t \cdot P_1 + 3 \cdot (1-t) \cdot t^2 \cdot P_2 + t^3 \cdot P_3, \quad (9)$$

where  $P_0$  – starting point;

$P_3$  – endpoint;

$P_1, P_2,$  and  $P$  – control points; operations on points  $P_i$  mean the same operations on each coordinate  $x_i$  and  $y_i$ . m.

We should parse the “d” parameter of the “path” commands. After that, we need to integrate products of functions. To avoid the realisation of all type combinations, we can convert all segments to cubic. It is very simple by expanding the corresponding equations into the monomial form and equating the coefficients at the same power at the parameter  $t$ . To convert a linear segment between points  $P_0$  and  $P_3$  to cubic, we need two control points  $P_1 = (P_3 + 2 \cdot P_0)/3$  and  $P_2 = (2 \cdot P_3 + P_0)/3$ . For a quadratic segment between points  $P_0$  and  $P_3$  with a control point  $P$  to cubic, we should cancel point  $P$  adding two control points  $P_1 = (P_0 + 2 \cdot P)/3$  and  $P_2 = (P_3 + 2 \cdot P)/3$ .

The most problematic tasks are taking  $y$  by  $x$  and integrating a product of curves. The first task requires the solution of the cubic equation (**Error! Reference source not found.**) in non-trivial cases using Viète’s trigonometric formula [22] and Holmes’s hyperbolic formulas [23] avoiding complex numbers. Integration of products is not trivial. A relation between parameters is required – a cubic equation, produced by equating the equations of  $x(t)$ . Numerical integration is used instead. The integrand is the product of the results of De Casteljaou’s [24] algorithm, applied to the solution of the cubic equation (**Error! Reference source not found.**) replacing  $B(t)$  by  $x$  and  $P_i$  by  $x_i$ . For the multiplication of Bezier curves, both are split to achieve corresponding nodes using De Casteljaou’s [24] algorithm.

Fig 1 d is built using the tabular data. It is not effective to approximate it by Bezier curves. In this work, a Hermit cubic spline is used by SciLab’s “splin” function. Not-a-knot conditions give higher approximation precision order if no additional artefacts (extremums, kinks) appear in some particular cases. To test this, the spline has been built using 100 points between the tabular ones (Fig 1 d). As no additional artefacts were found, the spline is accepted.

The software has been written in SciLab to parse Bezier-vectorized graphs in SVG format and integrate products of two Bezier curves or such curve and Hermit-spline-approximated tabular data. At first, the program parses the curve description in SVG and converts all non-cubic Bezier segments to cubic ones. The second stage is splitting both curves-multipliers to achieve the same ranges of segments by  $x$ . Because of the high plication of the curves in Fig. 1 a, b, the number of segments reaches hundreds. De Casteljaou’s [24] algorithm warrants preserving the curves. The third stage is the numerical integration using the “intg” function with the absolute/relative tolerance of  $10^{-13}/10^{-8}$ . For this, the integrand is coded as a function that takes any  $x$ -value, solves non-trivial or trivial cases of a cubic equation (9) with auto-selection of the corresponding formula (Viète’s, Holmes’s, quadratic, or linear equation solution) to find the parameter  $t$ , and calculates the corresponding  $y$ -value by equation (9) for the first curve. If the second curve is Bezier one, it repeats the steps above for the same  $x$ -value. If it is a Hermit spline, it uses “interp” to take the second multiplier. And finally, the function returns the product of both values of curves to the integration function.

## Results and Discussion

The integration using the software gives the values of the integrals: in formula (2) – 32.31374; in equation (3) – 103.0464; in expression (4) – 173.1475; in formulae (6) – 91.47271.

At  $K_m = 683.002 \text{ lm} \cdot \text{W}^{-1}$  [20], by equations (5) and (8)  $K_{ph} = 406.480 \text{ phlm} \cdot \text{W}^{-1}$  and  $\kappa = 1.68469 \text{ phlux} \cdot \text{lux}^{-1}$ , which fully defines phytocandela, phytolumen and phytolux allowing measurements by the cheapest and the most available devices – lux-meters. For rough measurements in solar energetics, which is a promising technology in Ukraine and the world [25-35], we can use the same approach applying the corresponding spectrums in full ranges. Also, we can see that candela cannot be a universal physical value. It is a more physiological one related to single biological species. Thus, it cannot be a base unit. If not, dB(A) is also a base unit as it has similar properties but for sound – dependent on the spectrum of perception and cannot be converted from other values directly.

## Conclusions

Known units used for plant illuminance are not fully complying with the plant physiology for modern artificial illumination with special spectrums. We propose using a new unit system – phytocandela-phytolumen-phytolux – according to the photosynthesis efficiency curve that is numerically equal to candela-lumen-lux under sunlight. It is an appropriate unit system for the illuminance of plants that allows keeping old recommendations for growing under sunlight. Integration of spectrums allows measuring illumination by the cheap and most available devices – lux-meters. We see that a candela is a unit belonging to single biological species and not a universal physical unit. Thus, it could not be a base unit.

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## Author contributions

Conceptualization, T.T.; methodology, T.T., V.M., A.M., I.P and V.K.; software, V.M.; validation, A.M., I.P and A.U.; formal analysis, V.M and V.K.; investigation, I.P., V.K. and A.U.; data curation, V.M. and A.U.; writing – original draft preparation, V.M.; writing – review and editing, T.T., A.M., I.P, V.K. and A.U.; project administration, T.T.; funding acquisition, T.T. All authors have read and agreed to the published version of the manuscript.

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